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# Heat capacity, enthalpy and entropy of ternary bismuth tantalum oxides

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# ABSTRACT

Heat capacity and enthalpy increments of ternary bismuth tantalum oxides  $Bi_4Ta_2O_{11}$ ,  $Bi_7Ta_3O_{18}$  and  $Bi_3TaO_7$  were measured by the relaxation time method (2–280 K), DSC (265–353 K) and drop calorimetry (622–1322 K). Temperature dependencies of the molar heat capacity in the form  $C_{pm}$ =445.8+0.005451T–7.489 ×  $10^6/T^2$  J K<sup>-1</sup> mol<sup>-1</sup>,  $C_{pm}$ =699.0+0.05276T–9.956 ×  $10^6/T^2$  J K<sup>-1</sup> mol<sup>-1</sup> and  $C_{pm}$ =251.6+0.06705T–3.237 ×  $10^6/T^2$  J K<sup>-1</sup> mol<sup>-1</sup> for Bi\_3TaO\_7, Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub> and for Bi<sub>7</sub>Ta<sub>3</sub>O<sub>18</sub>, respectively, were derived by the least-squares method from the experimental data. The molar entropies at 298.15 K,  $S^{\circ}_m$ (298.15 K)=449.6 ± 2.3 J K<sup>-1</sup> mol<sup>-1</sup> for Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub>,  $S^{\circ}_m$ (298.15 K)=743.0 ± 3.8 J K<sup>-1</sup> mol<sup>-1</sup> for Bi<sub>7</sub>Ta<sub>3</sub>O<sub>18</sub> and  $S^{\circ}_m$ (298.15 K)= 304.3 ± 1.6 J K<sup>-1</sup> mol<sup>-1</sup> for Bi<sub>3</sub>TaO<sub>7</sub>, were evaluated from the low-temperature heat capacity measurements.

## 1. Introduction

Ternary bismuth tantalum oxides (bismuth tantalates) are of considerable interest because they are constituents of practically important ternary systems SrO–Bi<sub>2</sub>O<sub>3</sub>–Ta<sub>2</sub>O<sub>5</sub> and Bi<sub>2</sub>O<sub>3</sub>–Ta<sub>2</sub>O<sub>5</sub>–Nb<sub>2</sub>O<sub>5</sub>. Ternary oxide SrBi<sub>2</sub>Ta<sub>2</sub>O<sub>9</sub> is one of the most promising candidates for lead-free non-volatile random access memory applications while solid solutions Bi(Ta,Nb)O<sub>4</sub> and Bi<sub>3</sub>(Ta,Nb)O<sub>7</sub> have found some technological applications such as microwave dielectrics or photocatalysts.

Phase relations in the Bi-rich part of binary system  $Bi_2O_3-Ta_2O_5$ have been studied by Zhou [1,2] and Ling et al. [3–6]. Using X-ray diffraction, selected area electron diffraction and high-resolution electron microscopy Zhou [2] identified a number of phases: tetragonal (Bi,Ta) $O_x$  solid solution,  $\delta$ -Bi<sub>2</sub> $O_3$  based cubic (Bi,Ta) $O_y$ solid solution in the composition range  $Bi_{19}TaO_{31}$ - $B_3TaO_7$  and four stoichiometric ternary oxides  $Bi_7Ta_3O_{18}$ ,  $Bi_4Ta_2O_{11}$ ,  $Bi_{31}Ta_{17}O_{89}$  and  $BiTaO_4$ . Atomic arrangements in these crystalline phases are rather complicated and superstructures of different symmetry were recognized. Similar findings were presented by Ling et al. [3,6] based on the X-ray diffraction and electron diffraction data. A refinement of the crystal structure of  $Bi_7Ta_3O_{18}$  was performed later [4] using single-crystal X-ray diffraction and powder neutron diffraction data. A triclinic (*P*1) crystal structure was assigned to  $Bi_7Ta_3O_{18}$  however a

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monoclinic (*C*2/*m*) crystal structure reproduced the experimental data comparably well. A triclinic (*P*-1) crystal structure was proposed for Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub> [5] based on synchrotron X-ray diffraction and powder neutron diffraction data. Crystal structure of Bi<sub>3</sub>TaO<sub>7</sub> was examined by X-ray and neutron powder diffraction by Abrahams et al. [7]. This oxide possesses a defect fluorite structure (*Fm*-3*m*). BiTaO<sub>4</sub> is known to exist in low-temperature (LT) orthorhombic structure and high-temperature (HT) triclinic structure [8–10]. The temperature of equilibrium transformation LT  $\leftrightarrow$  HT is not known but according to conditions used for the preparation of LT and HT modifications it falls into 1073–1173 K interval.

There is only one report [11] dealing with thermodynamic properties of Bi–Ta ternary oxides. Hampl et al. measured the heat capacity (2–570 K) and enthalpy increments (670–1170 K) of polycrystalline BiTaO<sub>4</sub> LT modification. The value of standard molar entropy at 298.15 K  $S_m$ (298.15 K)=149.11 J K<sup>-1</sup> mol<sup>-1</sup> was evaluated from low-temperature dependence of  $C_{pm}(T)$ . The aim of this work is the measurement of the heat capacity and enthalpy increments of bismuth tantalates Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub>, Bi<sub>7</sub>Ta<sub>3</sub>O<sub>18</sub> and Bi<sub>3</sub>TaO<sub>7</sub> in a broad temperature range and evaluation of the standard molar entropy of these ternary oxides at 298.15 K, as well as the temperature dependence of  $C_{pm}$  above room temperature.

# 2. Experimental

The samples were prepared by conventional solid state reactions from high purity  $Bi_2O_3$  (99.9%, Aldrich) and  $Ta_2O_5$  (99.85%,

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Alfa Aesar). The stoichiometric amounts of precursors were ground in agate mortar, pressed into pellets and fired at 1073 K in platinum crucible in air atmosphere for 48 h. After regrinding the pellets, the coarse powder was ball milled for 30 min at 500 rpm, pressed again and fired at 1103 K in air for 100 h. Phase composition of the prepared samples was checked by the X-ray powder diffraction (XRD). XRD data were collected at room temperature with an X'Pert PRO (PANalytical, the Netherlands)  $\theta - \theta$  powder diffractometer with parafocusing Bragg–Brentano geometry using CuKa radiation  $(\lambda = 1.5418 \text{ Å}, U = 40 \text{ kV}, I = 30 \text{ mA})$ . Data were scanned over the angular range  $5-60^{\circ}(2\theta)$  with an increment of  $0.02^{\circ}(2\theta)$  and a counting time of 0.3 s step $^{-1}$ . Data evaluation was performed by means of the HighScore Plus software package. To exclude a potential contamination of the prepared samples with Pt as a result of Bi<sub>2</sub>O<sub>3</sub> attack of crucible material at high temperatures the samples chemical composition was checked by X-ray fluorescent analysis (Axios, PANalytical, the Netherlands).

The PPMS equipment 14T-type (Quantum Design, USA) was used for the heat capacity measurements in the low-temperature region [12-16]. The measurements were performed by the relaxation method [17] with fully automatic procedure under high vacuum (pressure  $\sim 10^{-2}$  Pa) to avoid heat loss through the exchange gas. The samples were compressed into powder plates of approx. 4.4-12.6 mg. The densities of the pressed samples were about 65% of the theoretical ones. The samples were mounted to the calorimeter platform with cryogenic grease Apiezon N (supplied by Quantum Design). The procedure was as follows: First, a blank sample holder with the Apiezon only was measured in the temperature range approx. 2-280 K to obtain background data, then the sample plate was attached to the calorimeter platform and the measurement was repeated in the same temperature range with the same temperature steps. The sample heat capacity was then obtained as a difference between the two datasets. This procedure was applied, because the heat capacity of Apiezon is not negligible in comparison with the sample heat capacity ( $\sim$ 8% at room temperature) and exhibits a sol-gel transition below room temperature [18].

The manufacturer claims the precision of this measurement is better than 2% [19]; the control measurement of the copper sample (99.999% purity) confirmed this precision in the temperature range 50–250 K. However, the precision of the measurement strongly depends on the thermal coupling between the sample and the calorimeter platform. Due to unavoidable porosity of the sample plate this coupling is rapidly getting worse as the temperature raises above 270 K and Apiezon diffuses into the porous sample. Consequently, the uncertainty of the obtained data tends to be larger.

A Micro DSC III calorimeter (Setaram, France) in the incremental temperature scanning mode consisting of a number of 5-10 K steps (heating rate 0.2 K min<sup>-1</sup>) followed by isothermal delays of 9000 s was used for the heat capacity determination in the temperature

range 265–353 K. Synthetic sapphire, NIST Standard reference material No. 720, was used as the reference. The typical sample mass was 2.5–3.5 g. The uncertainty of heat capacity measurements is estimated to be better than  $\pm 1\%$ .

Enthalpy increment determinations were carried out by drop method using high-temperature calorimeter, Multi HTC 96 (Setaram, France). All measurements were performed in air by alternating dropping of the reference material (small pieces of synthetic sapphire, NIST Standard reference material No. 720) and of the sample (pressed pellets 5 mm in diameter) being initially held at room temperature, through a lock into the working cell of the preheated calorimeter. Endothermic effects are detected and the relevant peak area is proportional to the heat content of the dropped specimen. The measurements were performed at temperatures 622-1322 K on samples of 240-390 mg. The delays between two subsequent drops were 25-30 min. To check the accuracy of measurement, the enthalpy increments of platinum in the temperature range 770–1370 K were measured first and compared with published reference values [20]. The standard deviation of 22 runs was 0.47 kJ mol<sup>-1</sup>, the average relative error was 2.0%. Estimated overall accuracy of the drop measurements is  $\pm 3\%$ .

# 3. Results and discussion

The XRD analysis revealed that the prepared samples were without any observable diffraction lines from unreacted precursors or other phases (see the Supplementary Figs. S1–S3). The lattice parameters of the oxides were evaluated by Rietveld refinement [21] and are summarized in Table 1. Using the XRF analysis any Pt contamination exceeding  $\approx 10^{-2}$  wt% was ruled out.

The measured data used for further analysis for  $Bi_4Ta_2O_{11}$ involve 187  $C_{pm}$  values from relaxation time (2.3–267 K), 36 points from DSC (266–353 K) and 48 values of the enthalpy increments from the drop measurements (622–1271 K). For  $Bi_7Ta_3O_{18}$ , 88  $C_{pm}$ values from relaxation time (1.8–259.1 K), 36 points from DSC (266–353 K) and 29 values of the enthalpy increments from the drop measurement (672–1322 K) were obtained. Finally, 103  $C_{pm}$ values from relaxation time (1.9–287.5 K), 36 points from DSC (266–353 K) and 42 values of the enthalpy increments from the drop measurement (623–1271 K) were obtained for  $Bi_3TaO_7$ . All  $C_{pm}$  data are plotted in Fig. 1 and summarized in Supplementary Tables S1 and S2. Enthalpy increment data are shown in Fig. 2 and listed in Supplementary Table S3.

The fit of the low-temperature heat capacity data (LT fit) consists of two steps. Assuming the validity of the phenomenological formula  $C_{pm} = \beta T^3 + \gamma_{el} T$ , at  $T \rightarrow 0$  where  $\beta$  is proportional to the Debye temperature  $\Theta_D$  and  $\gamma_{el} T$  is the Sommerfeld term, we plotted the  $C_{pm}/T$  vs.  $T^2$  dependence for T < 8 K. The non-zero  $\gamma_{el}$  values (probably

Table	
Table	

Crystal structures, lattice parameters and densities of prepared powder samples.

Oxide	$Bi_4Ta_2O_{11}$		Bi <sub>7</sub> Ta <sub>3</sub> O <sub>18</sub>		Bi <sub>3</sub> TaO <sub>7</sub>		
	This work	01-089-4353 <sup>a</sup>	This work	01-089-6647 <sup>a</sup>	This work	00-044-0202ª	
Space group	P-1	P-1	C2/m	C2/m	Fm-3m	Fm-3m	
a (nm)	0.66159	0.66089	3.40162	3.40084	0.54593	0.54711	
b (nm)	0.76528	0.76569	0.76054	0.76069	0.54593	0.54711	
c (nm)	0.98781	0.98828	0.66354	0.66364	0.54593	0.54711	
$\alpha$ (deg.)	101.3926	101.3450	90.0	90.0	90.0	90.0	
$\beta$ (deg.)	90.0993	90.1830	109.1606	109.2380	90.0	90.0	
$\gamma$ (deg.)	89.9921	90.0290	90.0	90.0	90.0	90.0	
$d (g \text{ cm}^{-3})^{b}$	9.39	9.30	9.47	9.40	9.39	9.32	

<sup>a</sup> JCPDS reference code.

<sup>b</sup> Theoretical density calculated from the lattice parameters.

а

500

Drop-Exp #1

Drop-Exp #2



HT Fit 400 H<sub>m</sub>(T)-H<sub>m</sub>(298) (kJ/mol) ······ NKR 300 200 100 600 800 1000 1200 1400 T (K) b 800 Drop-Exp  $\diamond$ HT Fit 700 ----- NKR H<sub>m</sub>(T)-H<sub>m</sub>(298) (kJ/mol) 600 500 400 300 200 600 800 1000 1200 1400 T (K) С Drop-Exp 300 HT Fit ···· NKR 250 H<sub>m</sub>(T)-H<sub>m</sub>(298) (kJ/mol) 200 150 100 50 600 800 1000 1200 1400 T (K)

Fig. 1. Low-temperature heat capacity of  $Bi_4Ta_2O_{11}\left(a\right),Bi_7Ta_3O_{18}\left(b\right)$  and  $Bi_3TaO_7\left(c\right)$ .

Fig. 2. Enthalpy increments of Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub> (a), Bi<sub>7</sub>Ta<sub>3</sub>O<sub>18</sub> (b) and Bi<sub>3</sub>TaO<sub>7</sub> (c).

due to some metallic impurities or a series of Schottky-like transitions due to structure defects) are negligible in all cases ( $\sim$ 0.5 mJ K<sup>-1</sup> mol<sup>-1</sup>) and can be ignored in further analysis. Simultaneously, the  $C_{\rm pm}/T$  vs.  $T^2$  plot provides an estimation of  $\Theta_{\rm D}$ , as in this temperature range only the acoustic phonons are populated.

In the second step of the LT fit, both sets of the  $C_{pm}$  data (relaxation time+DSC) were considered. Analysis of the phonon heat capacity was performed as an additive combination of Debye and Einstein models. The phonon spectrum of a polyatomic compound contains three acoustic branches and 3n-3 optical ones,

where *n* is number of atoms per formula unit. In our case, i.e. 17  $(Bi_4Ta_2O_{11})$ , 28  $(Bi_7Ta_3O_{18})$  and 11  $(Bi_3TaO_7)$  atoms/f.u., this represents 48, 81 and 30 optical branches, respectively. (Let us note that this approach is still a simplification, since *n* should properly refer to the number of atoms per primitive unit cell.) However, this would lead to an inadequate increase of parameters to be fitted. To reduce the number of adjustable parameters, several individual branches are grouped together into multiple degenerate branches with the same characteristic temperatures using a trial-and-error method.

Both models include corrections for anharmonicity, which is responsible for a small, but not negligible, additive term at higher temperatures and which accounts for the discrepancy between isobaric and isochoric heat capacity. According to literature [22], the term  $1/(1 - \alpha T)$  is considered as a correction factor.

The acoustic part of the phonon heat capacity is then described using the Debye model in the form

$$C_{\rm phD} = \frac{9R}{1 - \alpha_{\rm D}T} \left(\frac{T}{\Theta_{\rm D}}\right)^3 \int_0^{x_{\rm D}} \frac{x^4 \exp(x)}{\left[\exp(x) - 1\right]^2} \,\mathrm{d}x \tag{1}$$

where *R* is the gas constant,  $\Theta_D$  is the Debye characteristic temperature,  $\alpha_D$  is the coefficient of anharmonicity of acoustic branches and  $x_D = \Theta_D/T$ . Here the three acoustic branches are taken as one triply degenerate branch. Similarly, the individual optical branches are described by the Einstein model

$$C_{\text{phE}i} = \frac{R}{1 - \alpha_{Ei}T} x_{Ei}^2 \frac{\exp(x_{Ei})}{\left[\exp(x_{Ei}) - 1\right]^2}$$
(2)

where  $\alpha_{Ei}$  and  $x_{Ei} = \Theta_{Ei}/T$  have analogous meanings as in the previous case. Several optical branches are again grouped into one degenerate multiple branch with the same Einstein characteristic temperature and anharmonicity coefficient. The phonon heat capacity then reads

$$C_{\rm ph} = C_{\rm phD} + \sum_{i=1}^{3n-3} C_{\rm phEi}$$
(3)

All the estimated values were included into the simplex routine [23] and a full non-linear fit was performed on all adjustable parameters. The analysis of the phonon heat capacity is summarized in Table 2.

The values of relative enthalpies at 298.15 K,  $H_m(298.15) - H_m(0)$ , for ternary bismuth tantalum oxides were evaluated from the low-temperature  $C_{pm}$  data (LT fit) by numerical integration of the  $C_{pm}(T)$  dependences from zero to 298.15 K. Standard deviations ( $2\sigma$ ) were calculated using the error propagation law. The values of standard molar entropies at 298.15 K,  $S_m(298.15)$ , were derived from the low-temperature  $C_{pm}$  data (LT fit) by numerical integration of the  $C_{pm}(T)/T$  dependences from zero to 298.15 K. A numerical integration of the  $C_{pm}(T)/T$  dependences from zero to 298.15 K. A numerical integration was used with the boundary conditions  $S_m = 0$  and  $C_{pm}/T = \gamma_{el}$  at T = 0 K. Standard deviations ( $2\sigma$ ) were calculated using the error propagation law. All calculated values are summarized in Table 3.

For the assessment of temperature dependencies  $C_{pm}$  above room temperature, the heat capacity data from DSC and the

Table 2					
Parameters	for	the	phonon	heat	capacity.

- - - -

enthalpy increment data from drop calorimetry were treated simultaneously (HT fit). Different weights  $w_i$  were assigned to individual points calculated as  $w_i = 1/\delta_i^2$  where  $\delta_i$  is the absolute deviation of the *i*th measurement estimated from overall accuracies of the measurements (1% for DSC and 3% for drop calorimetry). Both types of experimental data thus gain comparable significance during the regression analysis. To smoothly connect the LT fit and HT fit data the values of  $C_{pm}(298.15)$  from LT fit (see Table 3) were used as constraints. The temperature dependencies of the heat capacities of the investigated bismuth tantalates (T=298.15-1400 K) can thus be expressed by

Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub>

$$C_{pm} = (445.8 \pm 18.2) + (5.451 \pm 23.344) \times 10^{-3}T$$
$$-\frac{(7.489 \pm 1.020) \times 10^{6}}{T^{2}} \quad (JK^{-1} \text{ mol}^{-1})$$
(4)

Bi<sub>7</sub>Ta<sub>3</sub>O<sub>18</sub>

$$C_{pm} = (699.0 \pm 31.2) + (52.762 \pm 41.859) \times 10^{-3}T$$
$$-\frac{(9.956 \pm 1.704) \times 10^{6}}{T^{2}} \quad (JK^{-1}mol^{-1})$$
(5)

Bi<sub>3</sub>TaO<sub>7</sub>

$$C_{pm} = (251.6 \pm 14.6) + (67.05 \pm 19.34) \times 10^{-3}T$$
$$-\frac{(3.237 \pm 0.799) \times 10^{6}}{T^{2}} \quad (JK^{-1}mol^{-1})$$
(6)

The enthalpy increments as functions of temperature obtained by integration of  $C_{pm}(T)$  (HT fit, Eqs. (4)–(6)) are shown in Fig. 2. The pertinent dependencies deduced from  $C_{pm}(T)$  functions estimated according to the additive Neumann–Kopp's rule (NKR) are given for comparison. Applying NKR [24,25] the heat capacity of complex oxide is calculated as a linear combination of the heat capacities of constituent binary ones. In the case of bismuth tantalum mixed oxide  $x(Bi_2O_3).y(Ta_2O_5)$  we can write the following equations:

$$C_{pm}(x(Bi_2O_3)y(Ta_2O_5)) = xC_{pm}(Bi_2O_3) + yC_{pm}(Ta_2O_5)$$
(7)  
$$\Delta_{ox}C_{pm} = C_{pm}(x(Bi_2O_3)y(Ta_2O_5)) - xC_{pm}(Bi_2O_3) - yC_{pm}(Ta_2O_5) = 0$$

Temperature dependencies of  $\Delta_{ox}C_{pm}$  for BiTaO<sub>4</sub>, Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub>, Bi<sub>7</sub>Ta<sub>3</sub>O<sub>18</sub> and Bi<sub>3</sub>TaO<sub>7</sub> calculated according to Eq. (8) from experimental  $C_{pm}$  data for mixed oxides and literature  $C_{pm}$  data

Table 3

Standard thermodynamic functions for bismuth tantalates at 298.15 K.

Oxide	Bi <sub>4</sub> Ta <sub>2</sub> O <sub>11</sub>	Bi7Ta3O18	Bi <sub>3</sub> TaO <sub>7</sub>
$C_{pm}(298.15) (J K^{-1} mol^{-1}) H_m(298.15) - H_m(0) (J mol^{-1}) S_m(298.15) (J K^{-1} mol^{-1})$	$\begin{array}{c} 363.17 \\ 66566 \pm 384 \\ 449.6 \pm 2.3 \end{array}$	$\begin{array}{c} 602.74 \\ 109760 \pm 634 \\ 743.0 \pm 3.8 \end{array}$	$\begin{array}{c} 235.16 \\ 44265 \pm 254 \\ 304.3 \pm 1.6 \end{array}$

Oxide	Oxide Bi <sub>4</sub> Ta <sub>2</sub> O <sub>11</sub>			Bi <sub>7</sub> Ta <sub>3</sub> O <sub>18</sub>			Bi <sub>3</sub> TaO <sub>7</sub>		
Mode	$\Theta_i(\mathbf{K})$	$10^{5} \alpha_{i}  (\mathrm{K}^{-1})$	Degeneracy $(n=51)$	$\Theta_i(\mathbf{K})$	$10^{5} \alpha_{i}  (\mathrm{K}^{-1})$	Degeneracy (n=84)	$\Theta_i(\mathbf{K})$	$10^5 \alpha_i  ({ m K}^{-1})$	Degeneracy $(n=33)$
D	94	5	3	82	8	3	98	5	3
E1	91	5	6	73	9	8	91	10	4
E <sub>2</sub>	202	5	8	154	9	12	235	10	6
E <sub>3</sub>	257	9	10	256	12	16	271	15	6
E <sub>4</sub>	533	20	10	418	25	20	533	10	8
E <sub>5</sub>	759	20	14	820	30	25	899	10	6



**Fig. 3.** Temperature dependence of  $\Delta_{ox}C_{pm}$  for bismuth tantalum mixed oxides.

for Bi<sub>2</sub>O<sub>3</sub> [26] and Ta<sub>2</sub>O<sub>5</sub> [27] are shown in Fig. 3. It is obvious that NKR ( $\Delta_{ox}C_{pm}=0$ ) predicts the heat capacities of bismuth tantalum mixed oxides remarkably well around room temperature but in the case of Bi<sub>4</sub>Ta<sub>2</sub>O<sub>11</sub> and Bi<sub>3</sub>TaO<sub>7</sub> the deviations from NKR become substantial at high temperatures (above approx. 1200 K). Similar behavior was observed previously for strontium and calcium niobates [28–30] and can be explained by differences in dilatation terms due to molar volume contraction or expansion as well as the variation of thermal expansion and compressibility coefficients [25].

The obtained data were included into a thermodynamic database FeRAM [31] compatible with the FactSage software [32] which makes it possible to calculate various phase diagrams in the system  $CaO-SrO-Bi_2O_3-Nb_2O_5-Ta_2O_5$ .

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## Appendix A. Supplementary Material

Supplementary data associated with this article can be found in the online version at doi:10.1016/j.jssc.2010.11.020.

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